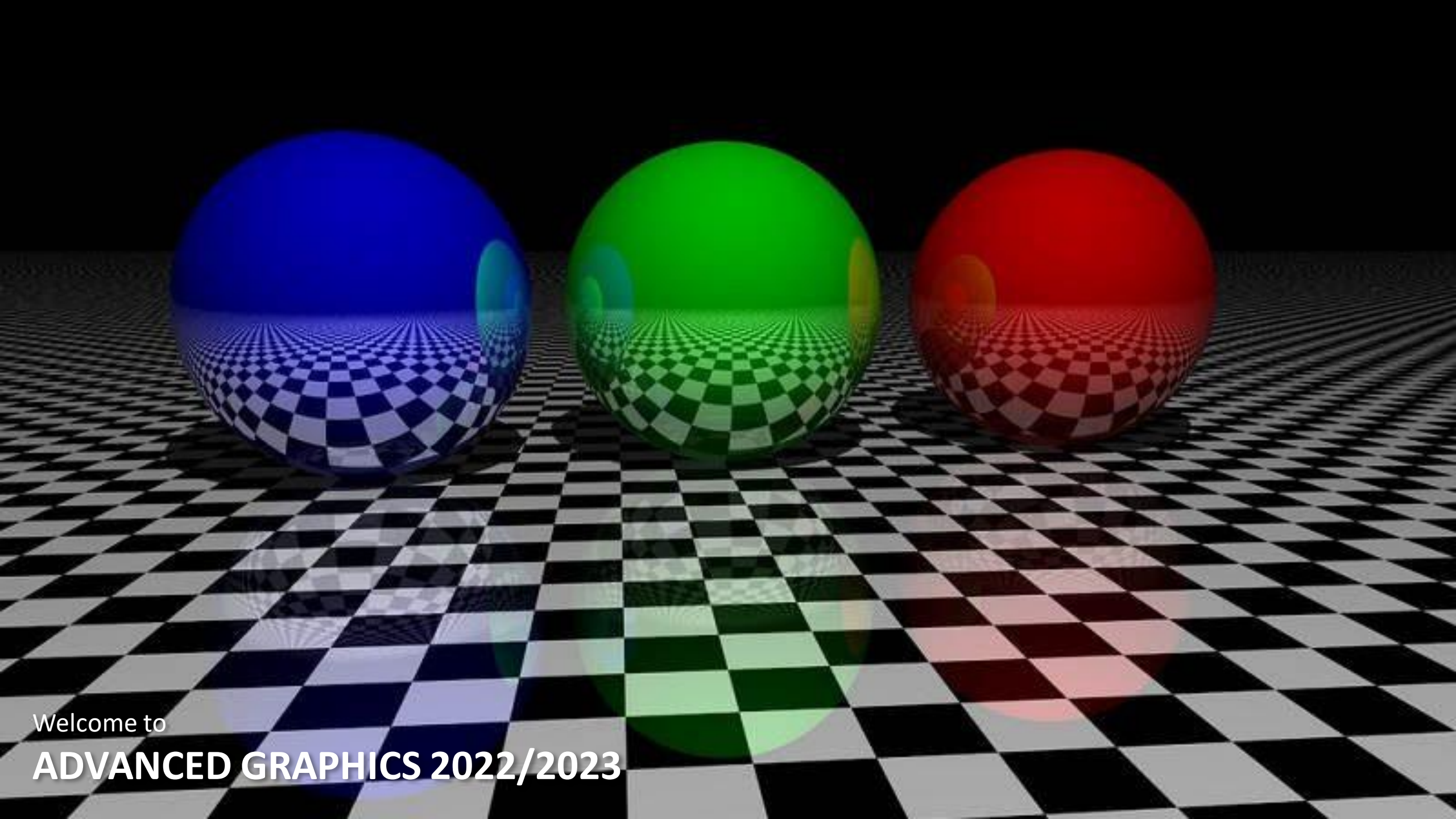




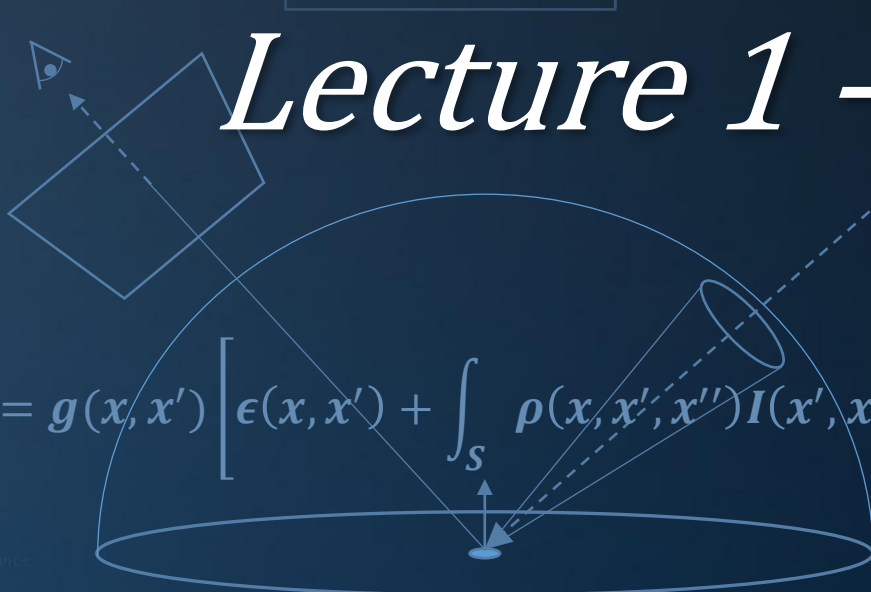
Welcome to
ADVANCED GRAPHICS 2022/2023

INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 - February 2023

Lecture 1 - “Introduction”

Welcome!


$$I(x, x') = g(x, x') \left[\epsilon(x, x') + \int_S \rho(x, x', x'') I(x', x'') dx'' \right]$$



Today's Agenda:

- Advanced Graphics
- Recap: Ray Tracing
- Assignment 1



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Website

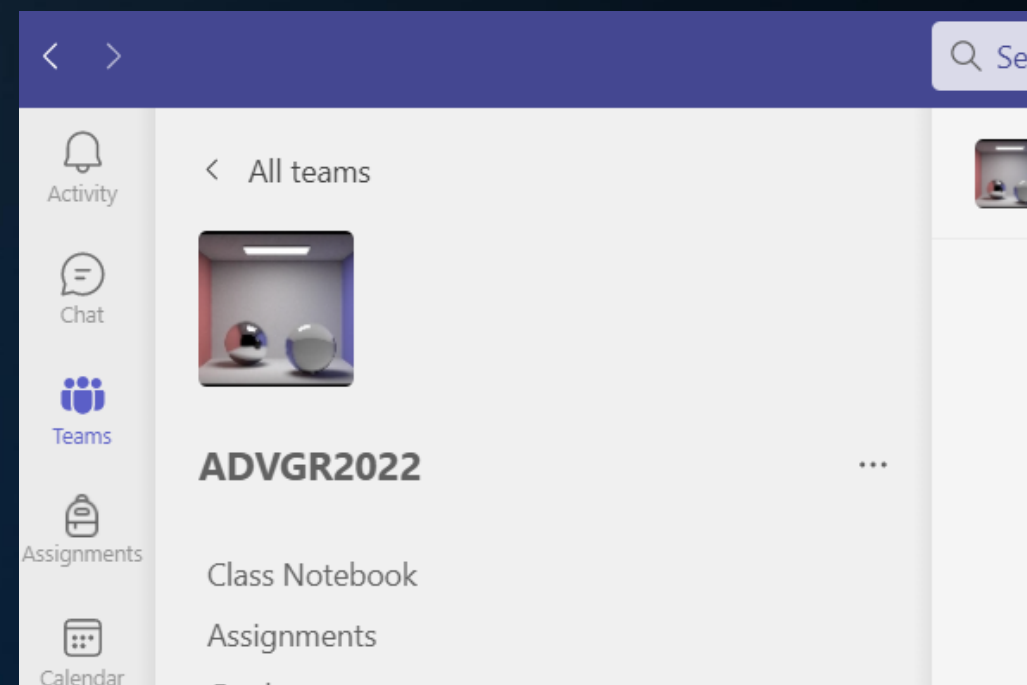
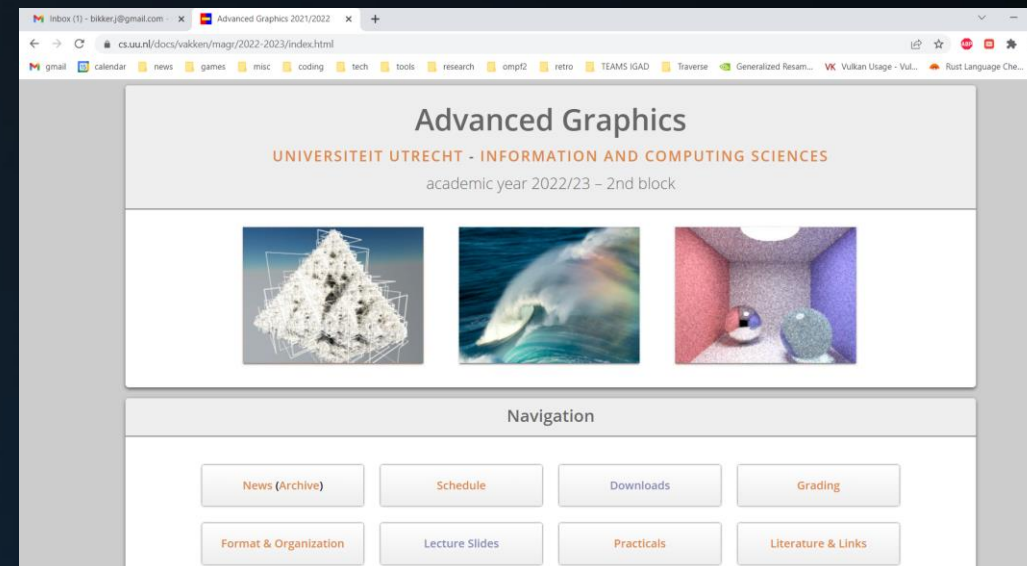
<http://www.cs.uu.nl/docs/vakken/magr>

- Downloads, news, slides, deadlines, links.
- Main source of information!
- Includes complex weekly room allocation.

Please check Teams for operational comms.

```

ics
& (depth < MAXDEPTH)
{
    if (nt < inside ? 1 : 0.5)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt * nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn *
    )
    E * diffuse;
    = true;
    }
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &align;
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Smith's
    ve)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &Psurvive;
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
  
```



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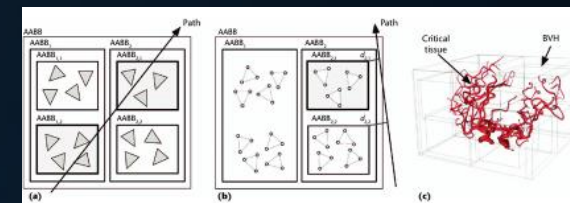
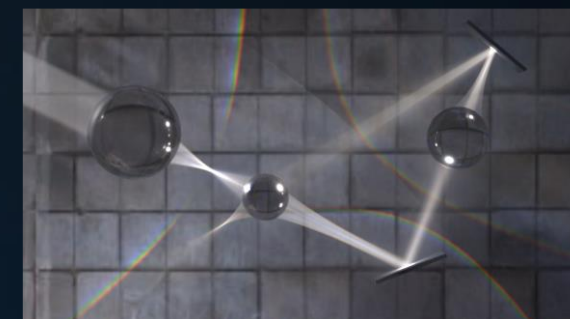
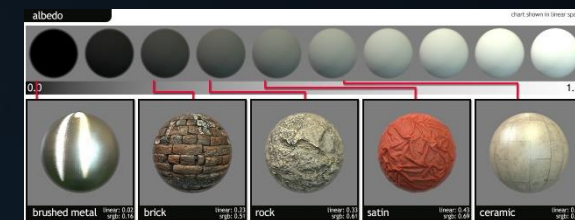
Abstract

In this course, we explore *Physically Based Rendering* (PBR), with a focus on *interactivity*.

At the end of this course, you will have a solid theoretical understanding of efficient physically based light transport using ray tracing and stochastic evaluation of the Rendering Equation (so: *no rasterization, sorry*).

You will also have a good understanding of acceleration structures for fast ray/scene intersection for static and dynamic scenes.

You will have hands-on experience with algorithms for efficient realistic rendering of static and dynamic scenes using ray tracing on CPU and GPU.



INFOMAGR

Abstract

In this course, we explore *physically based rendering*, with a focus on interactivity.

At the end of this course, you will have a solid theoretical understanding of efficient physically based light transport using ray tracing and stochastic evaluation of the Rendering Equation (so: *no rasterization, sorry*).

You will also have a good understanding of acceleration structures for fast ray/scene intersection for static and dynamic scenes.

You will have hands-on experience with algorithms for efficient realistic rendering of static and dynamic scenes using ray tracing on CPU and GPU.

Concrete / informal:

1. You'll know how a photo-realistic image is produced
2. You know how to do this quickly / efficient
3. You have built such a renderer
4. You have built an interactive ray tracer
5. You know how to do this on the GPU
6. You got a great score
7. You had fun

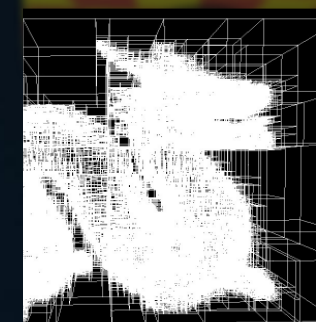
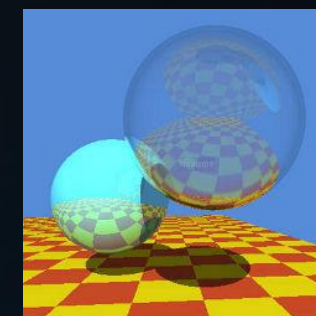
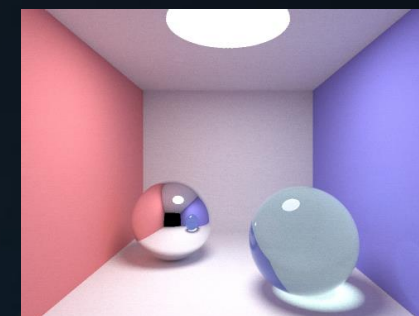


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Topics

We will cover the following topics:

- Ray tracing fundamentals;
- Whitted-style ray tracing;
- Acceleration structure construction;
- Acceleration structure traversal;
- Data structures and algorithms for animation;
- Stochastic approaches to AA, DOF, soft shadows, ... ;
- Path tracing;
- Variance reduction in path tracing algorithms;
- Filtering techniques;
- RTX / DXR (hardware options);
- State-of-the-art in ray tracing for games;
- Various forms of parallelism in ray tracing.



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Lectures

16 lectures:

Tuesday **10:00 – 11:45**, Thursday 13:15 – 15:00

Working colleges:

Tuesdays 09:00 – 10:00 (*1 hour, before the lecture*)

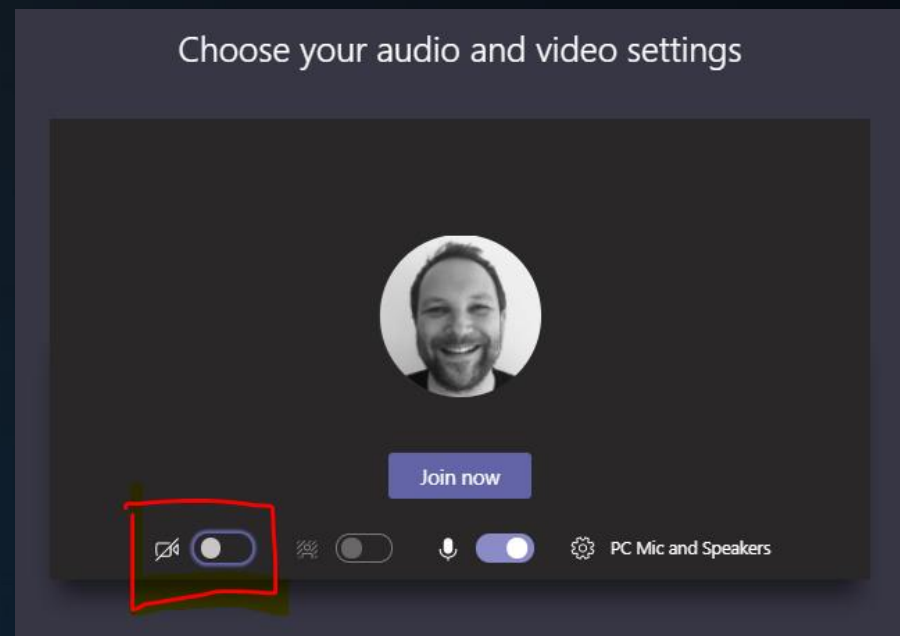
Thursdays 15:15 – 17:00 (*2 hours, after the lecture*)

All lectures are ON CAMPUS and will be recorded.

Slides will be made available, along with recordings.

Attendance is not mandatory, but of course highly recommended.

We move fast; missing a key lecture may be a serious problem.



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Literature

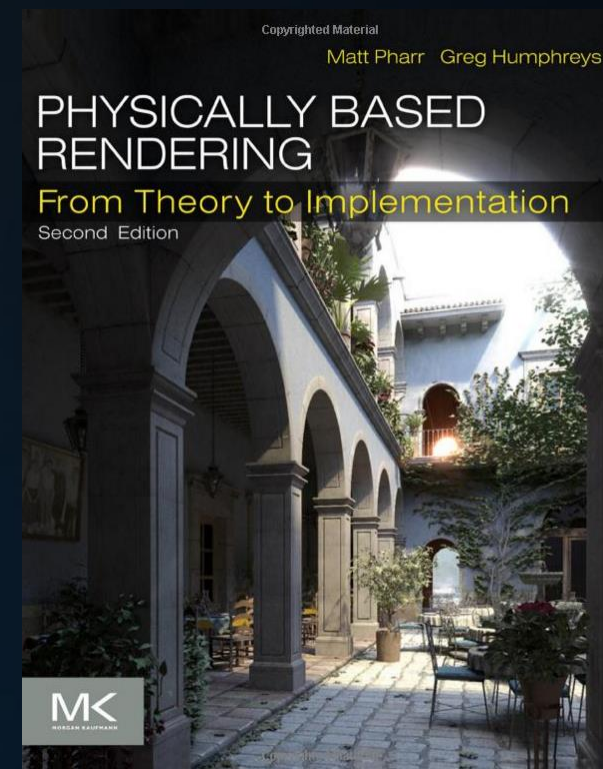
Papers and online resources will be supplied during the course.

Slides will be made available after each lecture.

Recommended literature:

Physically Based Rendering – From Theory to Implementation,
Pharr & Humphreys. ISBN-10: 9780128006450.

The 3rd edition is available for free: www.pbr-book.org



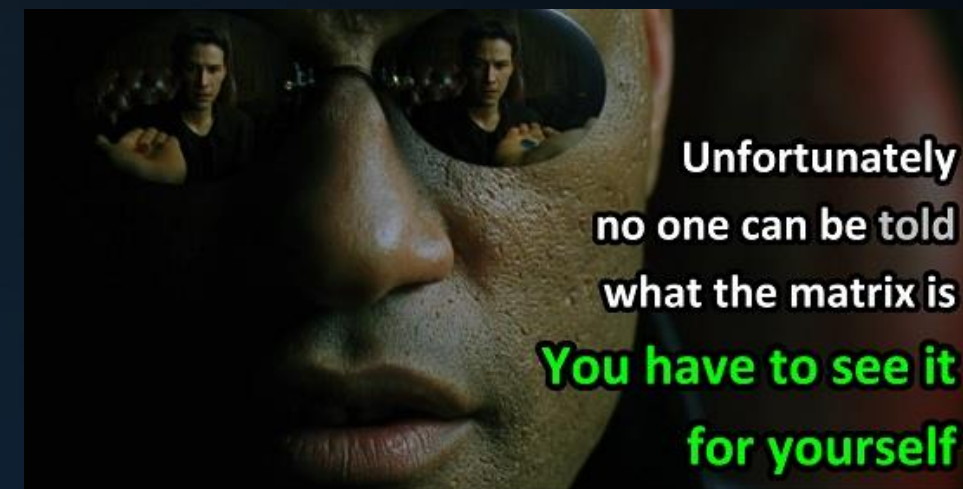
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Dependencies

It is assumed that you have basic knowledge of rendering (INFOGR) and associated mathematics.

You also should be a decent programmer; this is explicitly not a purely theoretical course. You are expected to verify the theory and experience the good and the bad.

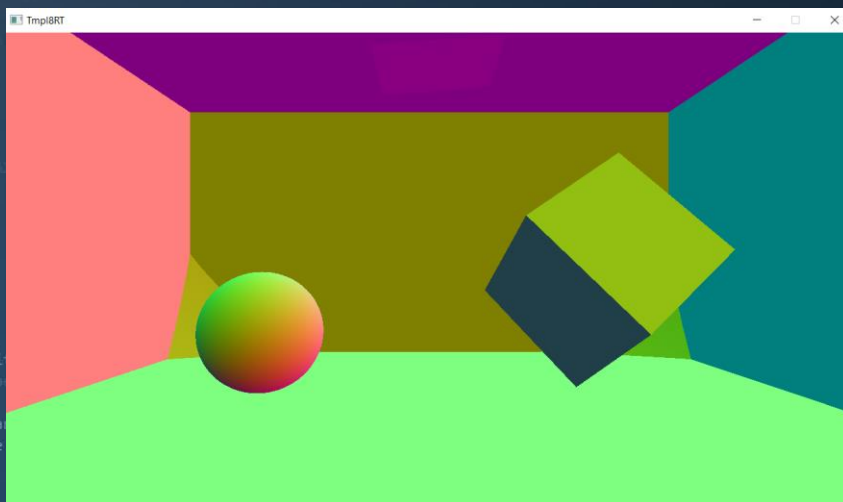
You can code in C/C++ or C# or Rust or basically any other Turing-complete language.



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Resources

You will develop a ray tracing testbed for assignment 1.
As a starting point, a 'template' is available.



However: feel free to use your own framework.



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Assignments

1. (weight: 1):
Light transport framework

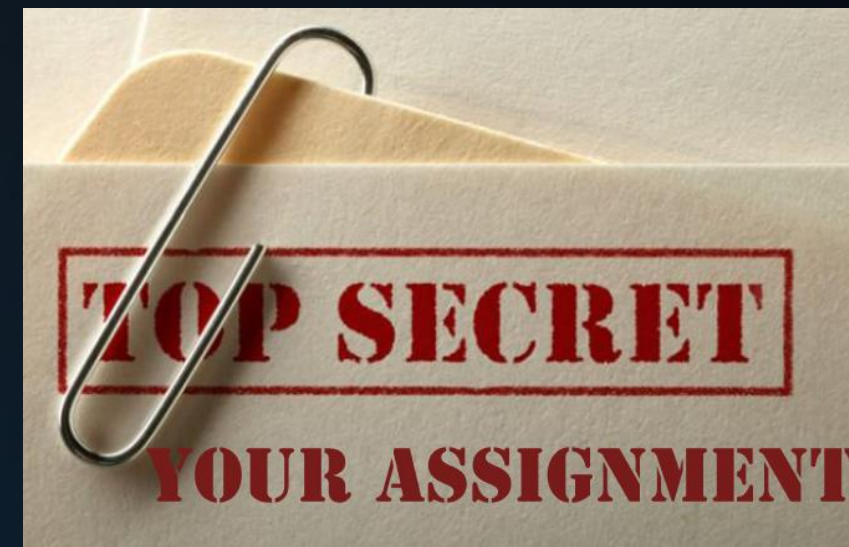
For this assignment, you prepare a testbed for subsequent assignments.

2. (weight: 1):
Acceleration structures

In this assignment, you expand your testbed with efficient acceleration structure construction and traversal. This enables you to run ray tracing in real-time (well...)

3. (weight: 2):
Final assignment

In this assignment, you either implement an interactive path tracer, or a rendering algorithm you chose, using CPU and/or GPU rendering.



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Exam

One final exam at the end of the block.

Materials to study:

- Slides
- Notes taken during the lectures
- Provided literature
- Assignments



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Grading & Retake

Final grade for assignments $P = (P1 + P2 + 2 * P3) / 4$

Final grade for INFOMAGR $G = (2P + E) / 3$

Passing criteria:

- $P \geq 4.50$
- $E \geq 4.50$
- $G \geq 5.50$

Repairing your grade using the retake exam or retake assignment:

- only if $5.50 > G \geq 4.00$
- you redo P1 or P2 or P3 or E
- this replaces the original P1, P2, P3 or E grade.



Today's Agenda:

- Advanced Graphics
- Recap: Ray Tracing
- Assignment 1



Recap

Ray

A ray is an infinite line with a start point:

$$P(t) = O + t\vec{D}, \text{ where } t \geq 0.$$

The ray direction $\vec{D}$ is usually normalized:
this way, t becomes a distance along the ray.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        r2t = 1.0f - nnt * nnt;
        D, N );
    }
    at a = nt - nc, b = nt * nc;
    at Tr = 1 - (R0 + (1 - R0) * r2t);
    (Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    E * diffuse;
    = true;
    defl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    if;
    radiance = SampleLight( &rand, I, &L, &light );
    e.x + radiance.y + radiance.z) > 0) && (dot(N, L) > 0)
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```



Recap

Ray Tracing

Primitives

```

float t = inside ? 1.0f : 0.0f;
float nt = nt / nc, ddn = ddn * nt;
float r0s2t = 1.0f - nnt * ddn;
float D, N );

```

```

float a = nt - nc, b = nt * nc;
float Tr = 1 - (R0 + (1 - R0) * r0s2t);
float R = (D * nnt - N * (ddn * r0s2t));

```

```

E * diffuse;
= true;

```

```

refl + refr)) && (depth < MAXDEPTH))

```

```

D, N );
refl * E * diffuse;
= true;

```

```

MAXDEPTH)

```

```

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following
if;

```

```

radiance = SampleLight( &rand, I, &L, &light );
e.x + radiance.y + radiance.z > 0) && (acc < 0.0001)

```

```

v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance

```

```

random walk - done properly, closely following Small's
ive)

```

```

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;

```

```

n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```

Scene

The scene consists of a number of primitives:

- Spheres
- Planes
- Triangles

...or anything for which we can calculate the intersection with a ray.

We also need:

- A camera (position, direction, FOV, focal distance, aperture size)
- Light sources

(ăp'ər-cher)



Recap

Ray Tracing

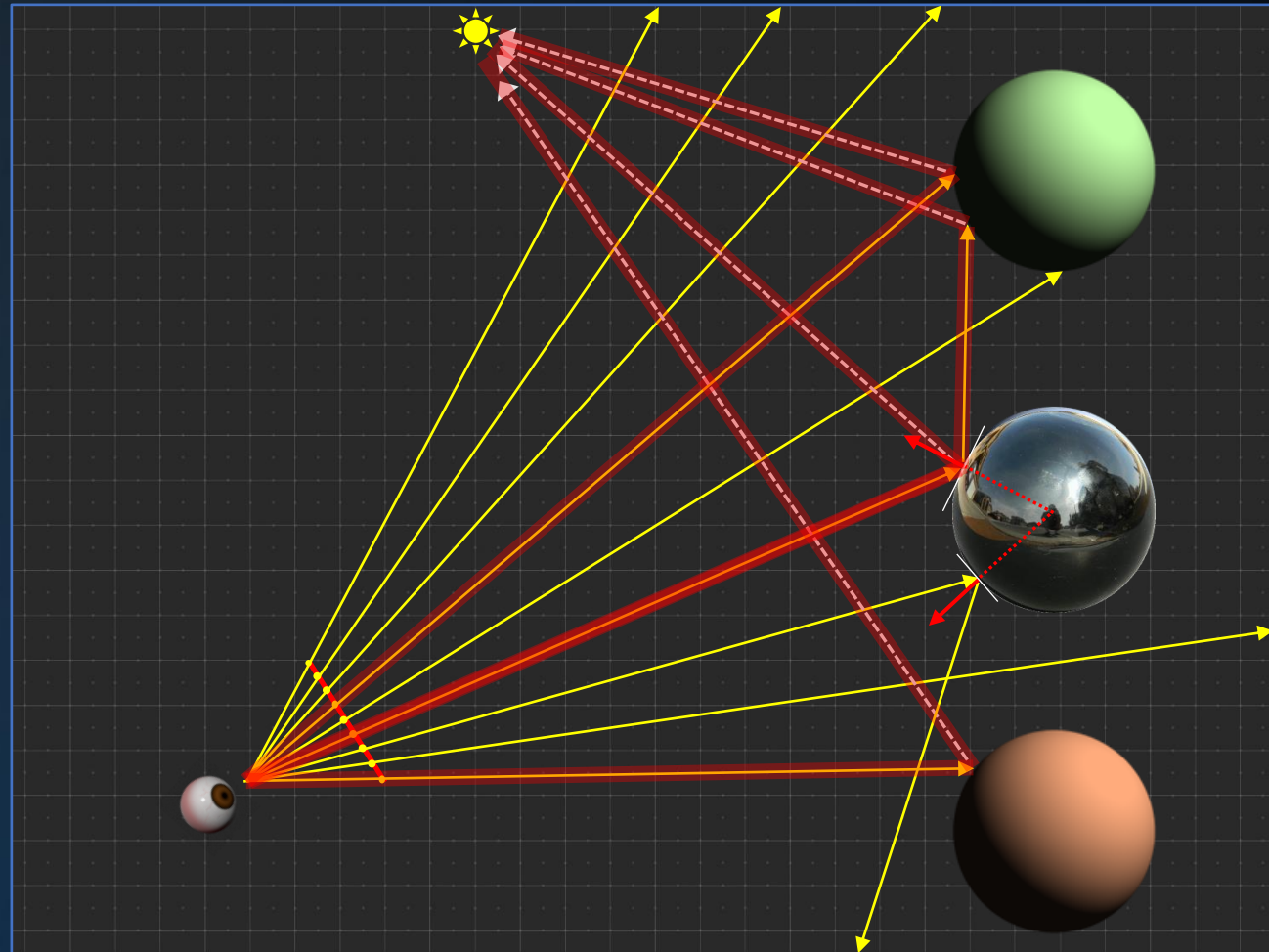
World space

- Geometry
- Eye
- Screen plane
- Screen pixels
- Primary rays
- Intersections
- Point light
- Shadow rays

Light transport

- Extension rays

Light transport



Recap

```

ics
& (depth < MAXDEPTH)
{
    if ( ! inside ) return 0;
    nt = nt / nc; ddn = ddn * ddn;
    cos2t = 1.0f - nnt * ddn;
    D, N );
    0);
    at a = nt - nc, b = nt * nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    efl + refr)) && (depth < MAXDEPTH)
    D, N );
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    MAXDEPTH)
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    estimation - doing it properly, closely
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    E * ((weight * cosThetaOut) / directPdf) * (radiant
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

Ray setup

A ray is initially shot through a pixel on the screen plane.
The screen plane is defined in *world space*, e.g.:

Camera position: $E = (0,0,0)$

View direction: $\vec{V} = (0,0,1)$

Screen center: $C = E + d\vec{V}$

Screen corners: $P_0 = C + (-1,-1,0), P_1 = C + (1,-1,0), P_2 = C + (-1,1,0)$

From here:

- Change FOV by altering d ;
- Transform camera by multiplying E, P_0, P_1, P_2 with a camera matrix.



Recap

Ray setup

Point on the screen:

$$P(u, v) = P_0 + u(P_1 - P_0) + v(P_2 - P_0)$$

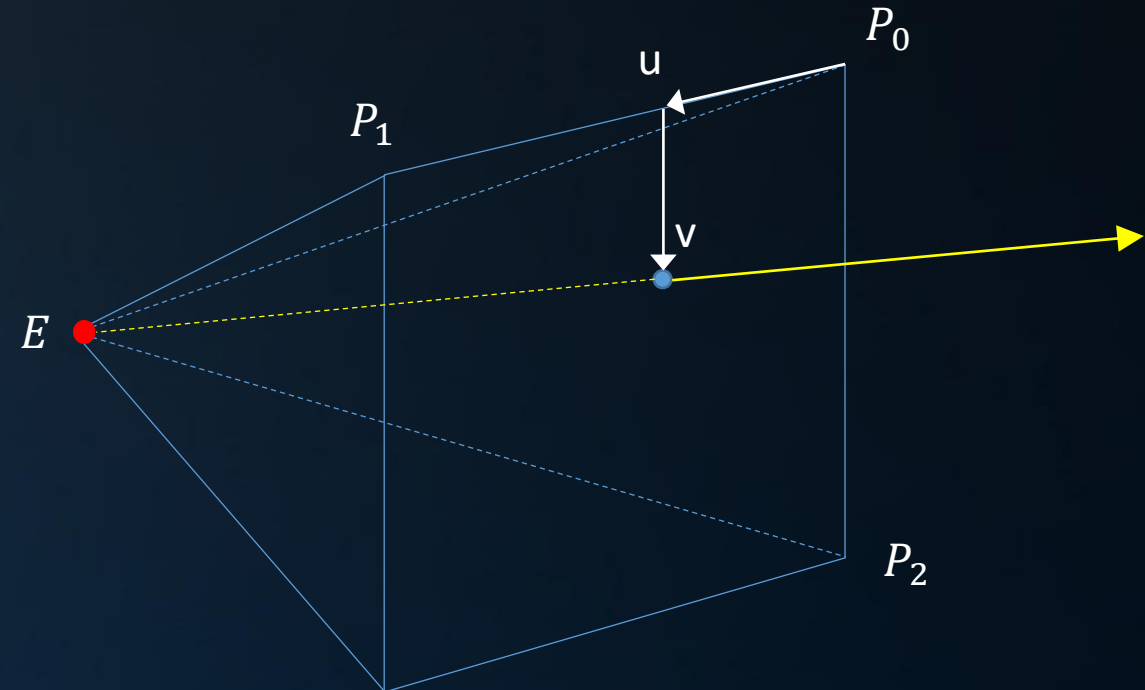
$$u, v \in [0, 1]$$

Ray direction (normalized):

$$\vec{D} = \frac{P(u, v) - E}{\|P(u, v) - E\|}$$

Ray origin:

$$O = E$$

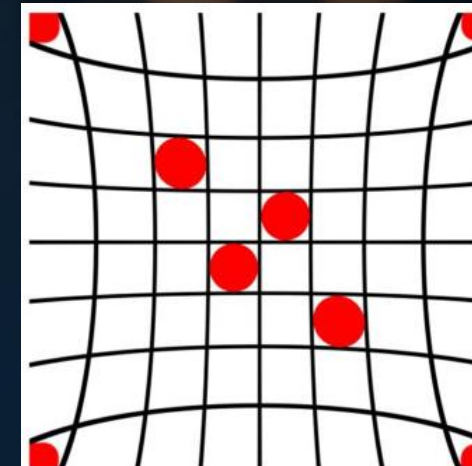


Recap

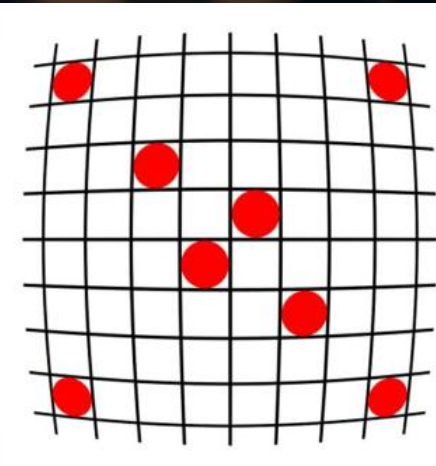
Ray setup

Alternatives:

- Taking into account HMD lens distortion



View through lens
(pincushion distortion)



Barrel distortion

Recap

Ray setup

Alternatives:

- Taking into account HMD lens distortion
- Fisheye lens

```

ics
& (depth < MAXDEPTH)
{
    if (inside) {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt * nc;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    R = (D * nnt - N * ddn);
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    df;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

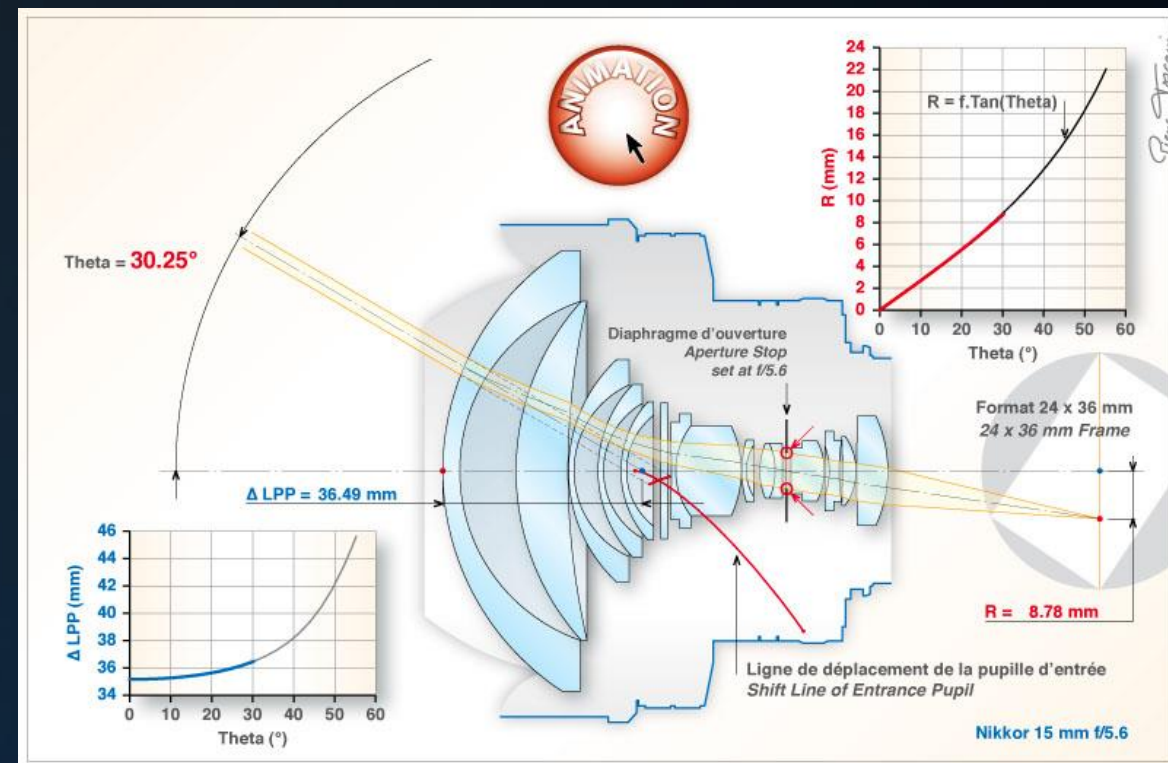


Recap

Ray setup

Alternatives:

- Taking into account HMD lens distortion
- Fisheye lens
- Complex lens system



Recap

Ray Intersection

Given a ray $P(t) = O + t\vec{D}$, we determine the closest intersection distance t by intersecting the ray with each of the primitives in the scene.

Ray / plane intersection:

Plane: $P \cdot \vec{N} + d = 0$

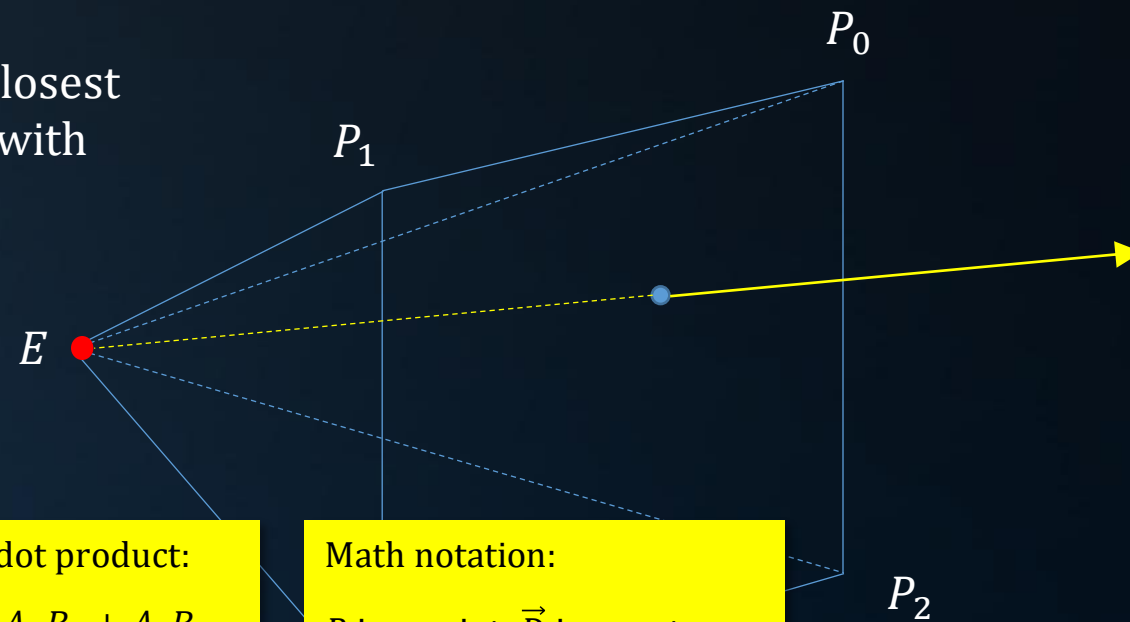
Ray: $P(t) = O + t\vec{D}$

Substituting for $P(t)$, we get

$$(O + t\vec{D}) \cdot \vec{N} + d = 0$$

$$t = -(O \cdot \vec{N} + d) / (\vec{D} \cdot \vec{N})$$

$$P = O + t\vec{D}$$



Math reminder, dot product:

$$A \cdot B = A_x B_x + A_y B_y + A_z B_z$$

$$A \cdot B = \cos \theta$$

$A \cdot B$ is: the *length* of the projection of A on B.

$A \cdot B$ is a *scalar*.

Math notation:

P is a point, $\vec{D}$ is a vector
 t is a scalar.



Recap

Ray Intersection

Ray / sphere intersection:

Sphere: $(P - C) \cdot (P - C) - r^2 = 0$

Substituting for $P(t)$, we get

$$(O + t\vec{D} - C) \cdot (O + t\vec{D} - C) - r^2 = 0$$

$$\vec{D} \cdot \vec{D} t^2 + 2\vec{D} \cdot (O - C) t + (O - C)^2 - r^2 = 0$$

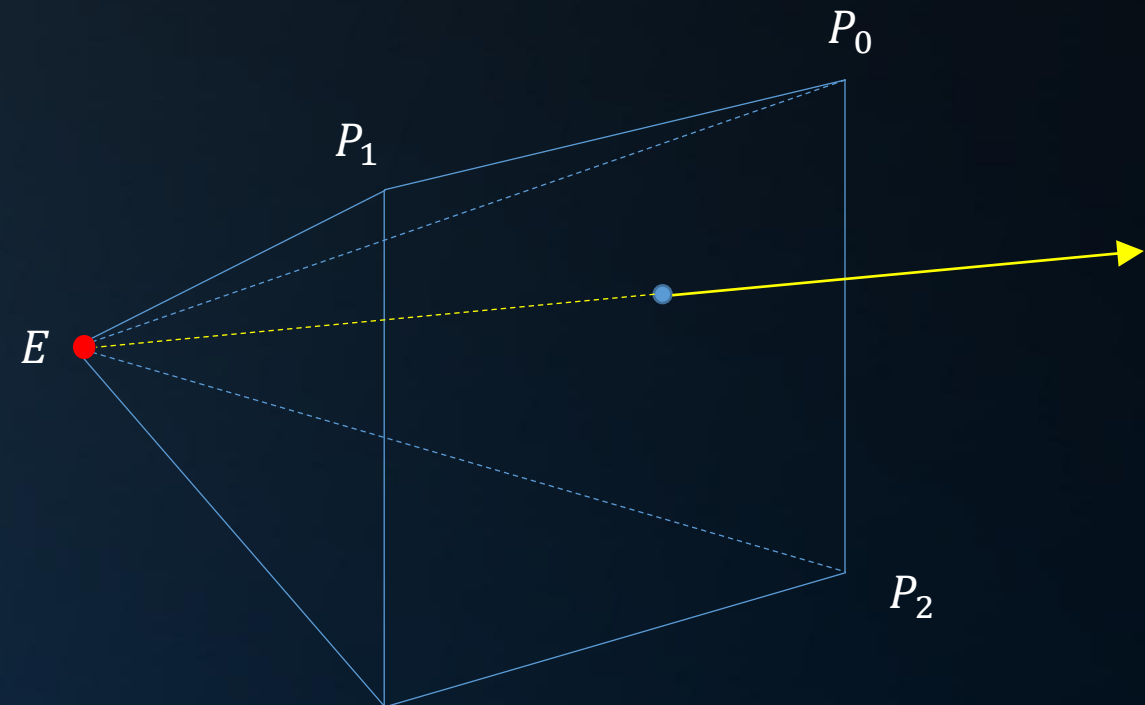
$$at^2 + bt + c = 0 \rightarrow t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = \vec{D} \cdot \vec{D}$$

$$b = 2\vec{D} \cdot (O - C)$$

$$c = (O - C) \cdot (O - C) - r^2$$

Negative:
no intersections



Recap

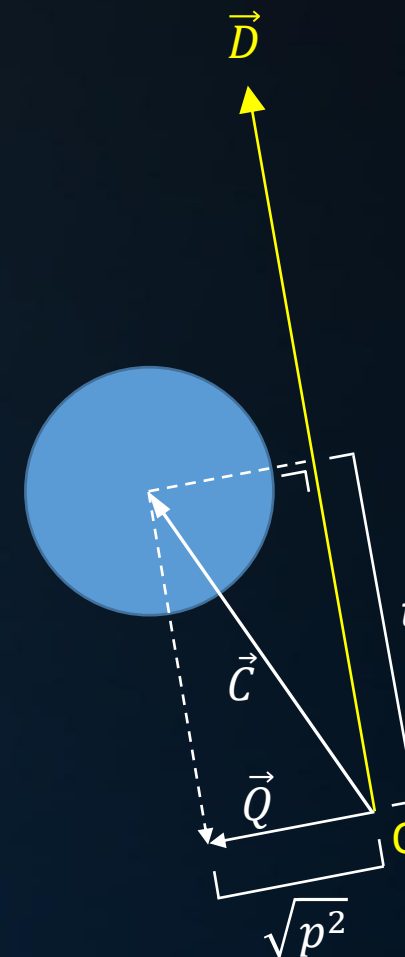
Ray Intersection

Efficient ray / sphere intersection:

```
void Sphere::IntersectSphere( Ray ray )
{
    vec3 C = this.pos - ray.O;
    float t = dot( C, ray.D );
    vec3 Q = C - t * ray.D;
    float p2 = dot( Q, Q );
    if (p2 > sphere.r2) return; // r2 = r * r
    t -= sqrt( sphere.r2 - p2 );
    if ((t < ray.t) && (t > 0)) ray.t = t;
}
```

Note:

This only works for rays that start outside the sphere.



Recap

Observations

Ray tracing is a *point sampling process*:

- we may miss small details;
- aliasing will occur.

Ray tracing is a *visibility algorithm*:

- For each pixel, we find the nearest object (which occludes objects farther away).

```

ics
& (depth < MAXDEPTH)
{
    if (inside) {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt * nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
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    = true;
    -
    efl + refr)) && (depth < MAXDEPTH)
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    = true;
    MAXDEPTH)
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    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light,
    e.x + radiance.y + radiance.z) > 0) && (dot(N, L)
    v = true;
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    at3 factor = diffuse * INVPI;
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    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;

```



Recap

Observations

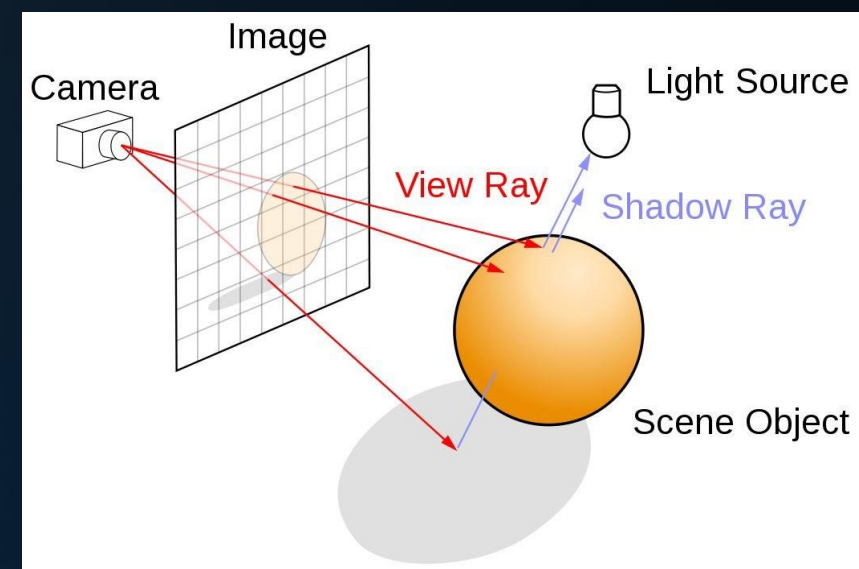
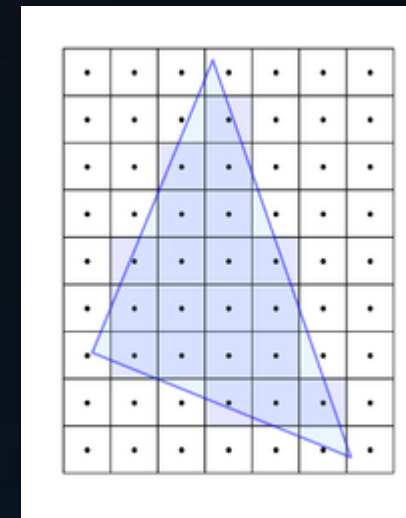
Note: rasterization (Painter's or z-buffer) is also a visibility algorithm.

Rasterization:

- loop over objects / primitives;
- per primitive: loop over pixels.

Ray tracing:

- loop over pixels;
- per pixel: loop over objects / primitives.



Today's Agenda:

- Advanced Graphics
- Recap: Ray Tracing
- Assignment 1

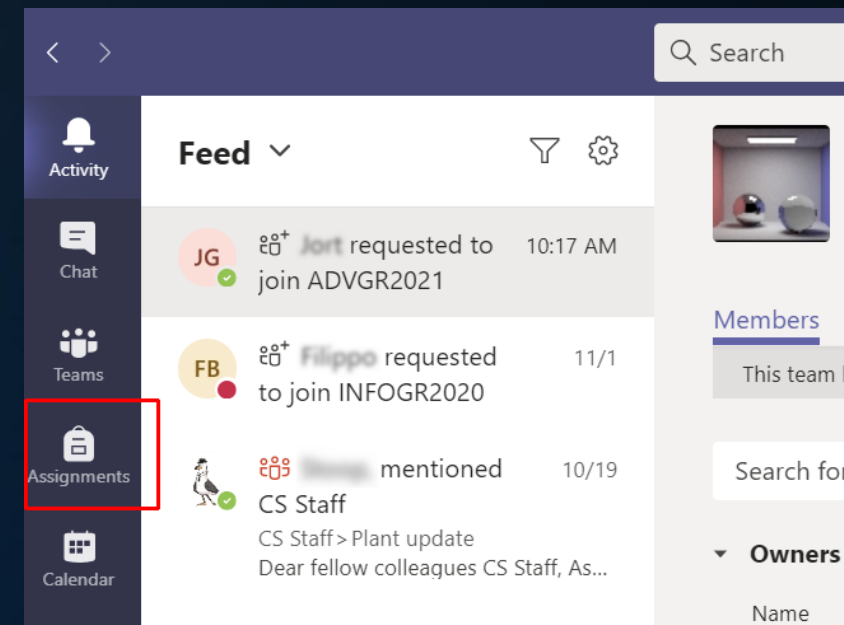
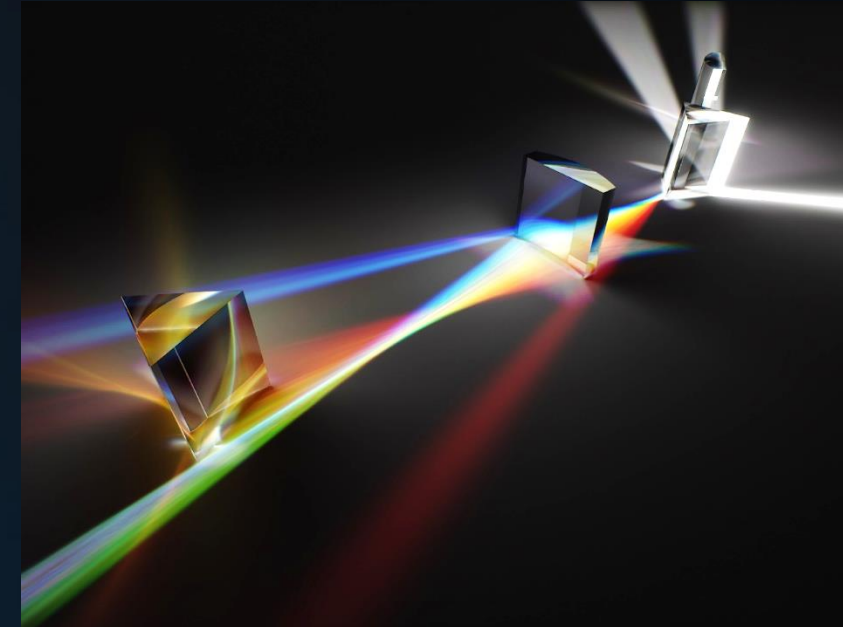


Assignment 1

Ray Tracing Testbed

Basic functionality of a ray tracer:

1. Calculate a color for each pixel on the screen
2. Do so using rays:
 - Start a ray at the camera location
 - Figure out where the pixel is in world space
 - Extend the (normalized) ray through the pixel
 - Find the nearest intersection (try them all)
 - Do fancy things at the nearest intersection.



Scene

I/O (e.g., obj loader)

Materials: diffuse color, diffuse / specular / dielectric, absorption

Position, target, FOV

Ray generation

Renderer

Whitted-style

Input handling

Presentation



Assignment 1

Ray Tracing Testbed

Regarding the file loading requirement:

- You may want to start with the included hardcoded scene
- Don't build your own OBJ loader, that's a waste of time
- Use assimp or tinyobjloader (C++) or find a lib if you're using C#

<http://www.stefangordon.com/parsing-wavefront-obj-files-in-c/>

<http://www.rexcardan.com/2014/10/read-obj-file-in-c-in-just-10-lines-of-code/>

<https://github.com/ChrisJansson/ObjLoader>

- Start with small scenes; minimize your development cycle.



Assignment 1

Ray Tracing Testbed

Intersecting triangles:

An easy to implement and quite efficient algorithm is:

Fast, Minimum Storage Ray/Triangle Intersection, Möller & Trumbore, 1997.

...which is explained in elaborate detail by [scratchapixel.com](http://www.scratchapixel.com/lessons/3d-basic-rendering/ray-tracing-rendering-a-triangle/moller-trumbore-ray-triangle-intersection):

<http://www.scratchapixel.com/lessons/3d-basic-rendering/ray-tracing-rendering-a-triangle/moller-trumbore-ray-triangle-intersection>

```

ics
& (depth < MAXDEPTH)
{
    float t = inside ? 1.0f : 0.0f;
    Vec nt = nt / nc, ddn = ddn * ddn;
    float cos2t = 1.0f - nnt * nnt;
    Vec D, N );
    Vec R = (D * nt - N * ddn) * cos2t;
    Vec a = nt - nc, b = nt * nc;
    float Tr = 1 - (R0 + (1 - R0) * cos2t);
    Vec R = (D * nt - N * ddn) * cos2t;
    Vec E * diffuse;
    Vec refl;
    Vec refl + refr)) && (depth < MAXDEPTH)
    Vec D, N );
    Vec refl * E * diffuse;
    Vec refl;
    Vec MAXDEPTH)
    Vec survive = SurvivalProbability( diffuse );
    Vec estimation - doing it properly, closely following Small's
    Vec if;
    Vec radiance = SampleLight( &rand, I, &L, &align, &pdf );
    Vec e.x + radiance.y + radiance.z > 0) && (depth < MAXDEPTH)
    Vec w = true;
    Vec at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    Vec at3 factor = diffuse * INVPI;
    Vec at weight = Mis2( directPdf, brdfPdf );
    Vec at cosThetaOut = dot( N, L );
    Vec E * ((weight * cosThetaOut) / directPdf) * (radiance
    Vec random walk - done properly, closely following Small's
    Vec survive)
    Vec ;
    Vec at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    Vec survive;
    Vec pdf;
    Vec n = E * brdf * (dot( N, R ) / pdf);
    Vec sion = true;

```



Today's Agenda:

- Advanced Graphics
- Recap: Ray Tracing
- Assignment 1



INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 – February 2023

END of “Introduction”

next lecture: “Whitted-style Ray Tracing”

